







(-x,y) Y (X,y) Ellipse has 4-fold symmetry So use a Set 4 Pixel function Only traverse 1st guadrant y (-×,-+) $\frac{1}{1 - 1} \frac{(x', y')}{x'} \frac{dy}{dx} (x', y') = -1$ $\frac{x^2}{r_x^2} + \frac{y^2}{r_y^2} = 1$ Step in X until dy <-1 Then Step in y DDA Algorithm (Region I) -- Step in X: $\Delta X = 1, \Delta Y = - X r_{Y}^{2} / y r_{X}^{2}$ $\frac{dy}{dx} = -\frac{xr_{y}^{2}}{yr_{x}^{2}}$ Each iteration: X= X+1 y= y- Xrx /yrx2 dy =- 1 at (x', y') So Solve for (x'y') DDA Algorithm (Region II) -- Step in y: $\Delta y=1$, $\Delta x = -yrx^{2}/xry^{2}$

Midpoint Ellipse Algorithm - (XK, YK) just plotted Region I: dy >-1 => 2ry x < 2ry y 9ĸ 櫃 4-1 Next point: $\{(x_k+1, y_k), top \\ (x_k+1, y_k-1), Bottom \}$ $\mathbf{Y}_{\mathbf{K}}$ 4k-1 Xk Xki Xk Xki Region II: dy <-1 Next point: $\begin{cases} (x_k, y_k-1), Left \\ (x_k+1, y_k-1), Right \end{cases}$ Define: Px= 2ry x, Py=2rx y Region I when P. - Py Ellipse function: $f \equiv \chi^{2} \Gamma_{y}^{2} + \gamma^{2} \Gamma_{\chi}^{2} - \Gamma_{\chi}^{2} \Gamma_{g}^{2} = 0 \Rightarrow (\chi, \gamma) \text{ on curve}$ $= F_{valuate} \text{ at } (\chi + 1, \gamma_{k} + 2) \qquad (Mid point) \qquad (> 0 \Rightarrow outside, choose BOT$

Evaluate Ellipse function at midpoint (X+1, Y=1/2): $f_{k} = r_{y}^{2} \left(x_{k} + 1 \right)^{2} + r_{x}^{2} \left(y_{k} - y_{k}^{2} \right)^{2} - r_{y}^{2} r_{y}^{2}$ Too complex -- Try to get recurrence relation: $f_{k+1} = f_k + \Delta f$ $f_{k+1} = f_k + \Delta f$ $f_{k+1} = f_k + f_k$ $f_{k+1} = f_k + f_k$ $f_{k+1} = f_k + f_k$ $\begin{array}{c} x_{k+1} = x_{k}+1 \\ y_{k+1} = \begin{cases} y_k \ (top) \\ y_{k-1} \ (Bottom) \end{cases}$ Top case: f_ = ry2 ((x+1)+1) + rx2 (y-2) -rx ry Result: $\Delta f = \Gamma_y^{-1}(2X_k+3)$ But $X_{k+1}^{-1} = (X_k+1)$, so $\Delta f = \Gamma_y^{-1}(2X_{k+1}+1)$ $\Delta f = P_x + \Gamma_y^{-1}$ Bottom case, f = ry2((x+1)+1)2+ry2((y-1)-K2)2-rx2ry2 Result: $\Delta f = r_{y}^{-2}(2x_{k}+3) + r_{y}^{-2}(-2y_{k}+2)$ But $X_{k+1} = X_{k}+1 & Y_{k+1} = Y_{k}-1$, so $\Delta f = r_{y}^{-2} + P_{x} - P_{y}$

Initial Volkes of f. Px, Py, when x=0, y=ry $f_{o} = r_{y}^{2} (o+1)^{2} + r_{x}^{2} (r_{y} - k_{z})^{2} - r_{y}^{2} r_{y}^{2}$ $f_{o} = r_{y}^{2} + r_{x}^{2} (k_{4} - r_{y})$ Also need initial values of $P_x \in P_y$ $R_y = 2r_y^2 x_y = 0$ $P_y = 2r_x^2 y_y = 2r_x^2 r_y$ Also need recurrence relations for $P_x \in P_y$ $P_x = 2r_y^2 \chi_k$ $P_x = 2r_y^2 (\chi_{t+1})$ $P_{t+1} = 2r_y^2 (\chi_{t+1})$ $P_{t+1} = (2r_x^2y_k)$ $P_{t+1} = (2r_x^2y_k$ $\frac{1}{50} \frac{\Delta R_{y}}{2} = \frac{1}{2} \frac{1}{72} \frac{1}$

Region Π - Just plotted (x_k, y_k) $\begin{cases} (x_k, y_{k-1}), Left case \end{cases}$ Next point $\{ (x_{k+1}, y_{k-1}), Right case \end{cases}$ $M_{id} point : (x_{k} + \frac{t_{2}}{t_{2}}, \frac{y_{i-1}}{t_{k}}) \Rightarrow f = r_{y}^{2} (x + \frac{t_{2}}{t_{2}})^{2} + r_{x}^{2} (y - 1)^{2} + r_{x}^{2} r_{y}^{2}$ (predictor flue) Assume last point in Region I was (x', y') -Results: $f_{int} = r_y^2 (x' + \frac{y}{2})^2 + r_x^2 (y' - i)^2 - r_x^2 r_y^2$ Next point: y = y - i $\Delta P_y = 2r_x^2$ $f > 0 \Rightarrow \Delta f = r_x^2 - P_y$ $f < 0 \Rightarrow x = x + i, \Delta f = r_x^2 - P_y + P_x$



Scan Converting other 2D Curves

DDA:

y = f(x); If we can differentiate it: dy/dx = f'(x) Step in x for parts of curve where dy/dx < 1 x = x + 1 y = y + f'(x)Step in y for parts of curve where dy/dx > 1 y = y + 1x = x + 1/f'(x)













































- on complexity of character
- Each stroke must be scan converted ==> more time to display
- Easily scaled and rotated arbitrarily
 - just transform each stroke

Example Character-Display Algorithms

- See CS-460/560 Notes Web Pages:
- ∠ Links to:
 - An illustration of how to display bitmapped characters
 - An illustration of how to display stroked characters









































