

Bir polinomun derecesi kadar koku vardir.

$$x+1=0 \rightarrow \text{tek koku var } x=-1$$

$$x^2-4=0 \rightarrow \text{iki koku var } x=-2, x=+2$$

$$x^2-5=0 \rightarrow \text{iki koku var } x=-2.236, x=2.236$$

$$x^2+3x+2=0 \rightarrow \text{iki koku var } x=-2, x=-1$$

$$x^2+1=0 \rightarrow \text{iki koku var } x=i, x=-i$$

$$x^2+4=0 \rightarrow \text{iki koku var } x=2i, x=-2i$$

$$x^2+5=0 \rightarrow \text{iki koku var } x=-2.236i, x=2.236i$$

$$x^2+2x+1=0 \rightarrow \text{iki koku var } x=-1, x=-1$$

$$x^2=0 \rightarrow \text{iki koku var } x=0, x=0$$

$$x^2-x=0 \rightarrow \text{iki koku var } x=0, x=1$$

Bir polinomun bir koku kompleks ise onun eslenigi de muhakkak koktur.

$$x^2+1=0 \rightarrow x=-i, x=-i$$

$$x^2+2x+2=0 \rightarrow x=-1-i, x=-1+i$$

$$x^2-6x+25=0 \rightarrow x=3+4i, x=3-4i$$

$$x^2+6x+25=0 \rightarrow x=-3+4i, x=-3-4i$$

$$x^2+4x+13=0 \rightarrow x=-2+2i, x=-2-3i$$

$$x^2-4x+13=0 \rightarrow x=2+2i, x=2-3i$$

Pay ve paydasi polinom olan kesirlere rasyonel kesirler denir. Bir rasyonel kesir paydanin koku kadar basit kesirlere ayrlabilir.

$$\frac{a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0}{x^m + b_{m-1} x^{m-1} + \dots + b_1 x + b_0} = \frac{a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0}{(x+x_1)(x+x_2)\dots(x+x_m)}$$

$$= \frac{A_1}{x+x_1} + \frac{A_2}{x+x_2} + \dots + \frac{B_1}{x+x_5} + \frac{B_2}{(x+x_5)^2} + \frac{B_3}{(x+x_5)^3} + \dots$$

A ve B lerin toplami m adet

Ornekler

$$\frac{5x+7}{x^2+3x+2} = \frac{2}{x+1} + \frac{3}{x+2}, \quad [\text{usler,kok,bolum}] = \text{residue}([5\ 7], [1\ 3\ 2])$$

$$\frac{5x-7}{x^2-3x+2} = \frac{2}{x-1} + \frac{3}{x-2}, \quad [\text{usler,kok,bolum}] = \text{residue}([5\ -7], [1\ -3\ 2])$$

$$\frac{2x+1}{x^2+3x+2} = \frac{3}{x+2} + \frac{-1}{x+1},$$

Kokler kompleks ise carpanlara ayirma isleminde paya gelen terimler de kompleks ve esleniktir.

$$\frac{6x+20}{x^2+4x+5} = \frac{3+4i}{x+2+i} + \frac{3-4i}{x+2-i}, \quad \frac{6x-4}{x^2-4x+5} = \frac{3+4i}{x-2+i} + \frac{3-4i}{x-2-i}$$

$$\frac{10x - 32}{x^2 - 4x + 8} = \frac{5 + 3i}{x - 2 - 2i} + \frac{5 - 3i}{x - 2 + 2i}$$

$$\frac{10x - 8}{x^2 - 4x + 8} = \frac{5 - 3i}{x - 2 - 2i} + \frac{5 + 3i}{x - 2 + 2i}$$

$$\frac{14x^2 - 74x + 72}{x^3 - 9x^2 + 28x - 40} = \frac{5 - 3i}{x - 2 - 2i} + \frac{5 + 3i}{x - 2 + 2i} + \frac{4}{x - 5}$$

[usler,kok,bolum] = residue ([14 -74 72], [1 -9 28 -40])

$$\frac{14x^2 + 26x - 8}{x^3 + x^2 - 12x + 40} = \frac{5 - 3i}{x - 2 - 2i} + \frac{5 + 3i}{x - 2 + 2i} + \frac{4}{x + 5}$$

$$\frac{16x^3 + 42x^2 - 6x + 72}{x^4 + 2x^3 - 11x^2 + 28x + 40} = \frac{5 - 3i}{x - 2 - 2i} + \frac{5 + 3i}{x - 2 + 2i} + \frac{4}{x + 5} + \frac{2}{x + 1}$$

$$\begin{aligned} \frac{12x^3 - 106x^2 + 434x - 440}{x^4 - 10x^3 + 57x^2 - 148x + 200} &= \frac{5 - 3i}{x - 2 - 2i} + \frac{5 + 3i}{x - 2 + 2i} + \frac{1 + 3i}{x - 3 - 4i} + \frac{1 - 3i}{x - 3 + 4i} \\ &= \frac{10x - 8}{x^2 - 4x + 8} + \frac{2x - 30}{x^2 - 6x + 25} \end{aligned}$$

$$\frac{3x + 1}{x^2 - 2x + 1} = \frac{3}{x - 1} + \frac{4}{(x - 1)^2}, \quad [\text{usler,kok,bolum}] = \text{residue} ([3 1], [1 -2 1])$$

$$\frac{7x + 9}{x^2 + 2x + 1} = \frac{7}{x + 1} + \frac{2}{(x + 1)^2} \quad \frac{10x}{x^2 + 2x + 1} = \frac{10}{x + 1} + \frac{-10}{(x + 1)^2}$$

$$\begin{aligned} \frac{17x^5 - 282x^3 - 153x^2 + 1172x + 344}{x^6 - 4x^5 - 15x^4 + 50x^3 + 100x^2 - 168x - 288} &= \frac{1}{x + 2} + \frac{5}{(x + 2)^2} + \frac{6}{(x + 2)^3} \\ &\quad + \frac{7}{x - 3} + \frac{8}{(x - 3)^2} + \frac{9}{(x - 4)} \end{aligned}$$