

## VECTORLER

```
>>a=[ 7 2 5 ], b=[ 9 0 3 ]
>>c=1:5
c= 1 2 3 4 5

>>d=5:8
d= 5 6 7 8

>>e=0:2:10
0 2 4 6 8 10

>>f=0:0.1:0.6
0 0.1 0.2 0.3 0.4 0.5 0.6
```

```
>>g=zeros(1,6)
0 0 0 0 0 0

>>h=zeros(1,4)
0 0 0 0
```

```
>>k=ones(1,7)
1 1 1 1 1 1 1
```

```
>>m=ones(1,3)
1 1 1
```

## TOPLAMA ve CIKARMA

```
>>a=[ 2 8 10], b=[ 1 4 3]
```

```
>>c=a+b
2 8 10
+ 1 4 3
-----
3 12 13

c=[ 3 12 13]
```

```
>>d=10*a
d=[ 20 80 100]

>>e=5*b
5 20 15
```

```
>>f=10*a + 5*b
25 100 115
```

```
>>g= a-b
2 4 7
```

## VEKTORLERIN IC ICE KONULMASI

```
>>h=[ 1:5 ]
1 2 3 4 5
```

```
>>k=[ 1:5 1:3 ]
1 2 3 4 5 1 2 3
```

```
>>m=[ 0:2:10 10:3:22 ]
0 2 4 6 8 10 13 16 19 22
```

```
>>a=[ 8 10 3 ], b=[ 4 7 8 ]
>>c=[ a b ]
8 10 3 4 7 8
```

```
>>d=[ a a a ]
8 10 3 8 10 3 8 10 3
```

## Kompleks vectors

```
>>a=[ 3+4*j -6+9*j 2+5*j -7*j 30]
```

```
>>w=abs(a)
5 10.81 5.38 7 30
```

$\sqrt{3^2 + 4^2} = 5$ ,  $\sqrt{6^2 + 9^2} = 10.81 \dots$

```
>>p=angle(a)
0.92 2.15 1.19 -1.57 0
```

```
>>s=angle(a)*180/pi
53.13 123.69 68.19 -90 0
```

$$\tan^{-1}\left(\frac{4}{3}\right) = 0.92 \text{ radian} = 53.13^\circ$$

$$\tan^{-1}\left(\frac{9}{-6}\right) = 2.15 \text{ radian} = 123.69^\circ$$

## MATRISLER:

Asagidakileri yazın

```
>>a=[10 20 30; 40 50 60; 100 80 90];
```

```
>>b=[ 1 2 3; 4 5 6; -2 8 9];
```

```
c=[15 25 35];
```

$$a = \begin{bmatrix} 10 & 20 & 30 \\ 40 & 50 & 60 \\ 100 & 80 & 90 \end{bmatrix}, b = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ -2 & 8 & 9 \end{bmatrix},$$

$$c = [15 \quad 25 \quad 35],$$

Toplama, Cikarma, Carpma, Bolme, normal islemler gibi yapilir.

```
>>qq=a+b, ww=a-b; ee=a*d;
```

$$qq = \begin{bmatrix} 11 & 22 & 33 \\ 44 & 55 & 66 \\ -98 & 88 & 99 \end{bmatrix}, ww = \begin{bmatrix} 9 & 18 & 27 \\ 36 & 45 & 54 \\ 102 & 72 & 81 \end{bmatrix}, ee = \begin{bmatrix} 200 \\ 440 \\ 710 \end{bmatrix}$$

' isareti matris transpozesi icin kullanilir.

```
>>m=[ 1 2 3; 4 5 6 ], n=a', d=[ 1 2 5 ]'
```

$$m = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} \quad n = \begin{bmatrix} 1 & 4 \\ 2 & 5 \\ 3 & 6 \end{bmatrix}, \quad d = \begin{bmatrix} 1 \\ 2 \\ 5 \end{bmatrix}$$

### Satir ve Sutun islemleri

Asagidaki ifadeleri yazin ve G matrisini ekranda gorun

```
>> G=[10 20 30 40; 210 220 230 240 ; 310 320 330 340;
410 420 430 440];
```

$$G = \begin{bmatrix} 10 & 20 & 30 & 40 \\ 210 & 220 & 230 & 240 \\ 310 & 320 & 330 & 340 \\ 410 & 420 & 430 & 440 \end{bmatrix}$$

Asagidaki ifadeleri yazin ve sonucları ekranda gorun

```
>> h=G(:,1), k=G(:,2), m=G(:,4), n=G(1,:),
p=G(2,:);
```

$$h = \begin{bmatrix} 10 \\ 210 \\ 310 \\ 410 \end{bmatrix}, k = \begin{bmatrix} 20 \\ 220 \\ 320 \\ 420 \end{bmatrix}, m = \begin{bmatrix} 40 \\ 240 \\ 340 \\ 440 \end{bmatrix},$$

$$n = [10 \quad 20 \quad 30 \quad 40]$$

$$p = [410 \quad 420 \quad 430 \quad 440]$$

Ayrica , r=G(1:2,:), t=G(:,1:2), s=G(1:2,1:2)

$$r = \begin{bmatrix} 10 & 20 & 30 & 40 \\ 210 & 220 & 230 & 240 \end{bmatrix}, t = \begin{bmatrix} 10 & 20 \\ 210 & 220 \\ 310 & 320 \\ 410 & 420 \end{bmatrix},$$

$$s = \begin{bmatrix} 10 & 20 \\ 210 & 220 \end{bmatrix},$$

```
>> aa=1:10
```

$$aa = [1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6 \quad 7 \quad 8 \quad 9 \quad 10]$$

```
>> aa=1:7, bb=sin(aa),
```

$$bb = [0.84 \quad 0.9 \quad 0.14 \quad -0.75 \quad -0.95 \quad -0.27 \quad 0.65]$$

her elemanin ayri ayri sinusu alinir

$$bb = [\sin(1) \quad \sin(2) \quad \sin(3) \quad \sin(4) \quad \sin(5) \quad \sin(6) \quad \sin(7)];$$

Matrices can be nested into each other. Examine the following examples.

```
>> a=[1 2 3]; b=[10 100 200]; c=[11 22 33]; d=[a; b; c];
e=[a b c];
```

$$d = \begin{bmatrix} 1 & 2 & 3 \\ 10 & 100 & 200 \\ 11 & 22 & 33 \end{bmatrix},$$

$$e = [1 \quad 2 \quad 3 \quad 10 \quad 100 \quad 200 \quad 11 \quad 22 \quad 33]$$

```
>> a=[1 2; 3 4]; b=[a [10 20]'; 7 8 9]
```

$$a = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}, b = \begin{bmatrix} 1 & 2 & 10 \\ 3 & 4 & 20 \\ 7 & 8 & 9 \end{bmatrix}$$

MATLAB da tanimlanmis fonksiyonlar

**zeros(n,m)** n x m boyutlu, tum elemanlari sifir matrix

**ones(n,m)** n x m boyutlu, tum elemanlari 1 matrix

**eye(n)** n x n boyutlu birim matris. tum elemanlari 0 sadece kosegen elemanlari 1.

**size(qq)** Bir matrisin boyutlarini verir. m ve n yi verir

**qq'** Transpose of the matrix qq

**inv(qq)** matris tersi (inversi)

**diag(qq)** diagonal of the matrix qq

**sum(qq)** sutunlarin toplamı

**det(qq)** determinant of the matrix qq.

### Example 1)

```
>> ww=ones(2,3), ff=zeros(3,4), gg=eye(3),
```

$$ww = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}, ff = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix},$$

$$gg = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

### Example 2)

```
>> [wrow wcolum]=size(ww),
wrow=2 wcolum=3
```

```
>> [frow fcolum]=size(ff),
```

$$\text{frow}=3 \quad \text{frow}=4$$

### Example 3)

```
>> q=[1 2; 3 4], p=[10 20; 30 40];
```

$$r=[ \quad q \quad \text{zeros}(2,2) ] \quad [\text{ones}(2,2) \quad p]]$$

$$q = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}, \quad r = \begin{bmatrix} 10 & 20 \\ 30 & 40 \end{bmatrix},$$

$$r = \begin{bmatrix} 1 & 2 & 0 & 0 & 1 & 1 & 10 & 20 \\ 3 & 4 & 0 & 0 & 1 & 1 & 30 & 40 \end{bmatrix}$$

### Example 4)

```
>> e = [ zeros(1,4) ones(1,3) ]
```

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 1 & 1 & 1 \end{bmatrix}$$

```
>> e = [ zeros(1,4) ones(1,3) ]
```

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 1 & 1 & 1 \end{bmatrix}$$

```
>> f = [ ones(1,3) 10*ones(1,4) ]
   1 1 1 10 10 10 10
```

```
>> g = 10*[1:3]
   10 20 30
```

```
>> h = [ ones(1,3) 10:2:20]
   1 1 1 10 12 14 16 18 29
```

```
>> k =[ 10*ones(1,3) 17 10:3:19 ]
   10 20 30 17 10 13 16 19
```

```
>> f = [ ones(1,3) 10*ones(1,4) ]
   1 1 1 10 10 10 10
```

```
>> g = 10*[1:3]
   10 20 30
```

```
>> h = [ ones(1,3) 10:2:20]
   1 1 1 10 12 14 16 18 29
```

```
>> k =[ 10*ones(1,3) 17 10:3:19 ]
   10 20 30 17 10 13 16 19
```

### Example 5)

```
>> aa=[4 6 0 0 2 2 40 60]
```

```
>> bb=sum(aa)
```

$$bb=114$$

vektorun tum elemanlari toplandi.

$$4 + 6 + 0 + 0 + 2 + 2 + 40 + 60 = 114$$

### Example 6)

Most built-in functions (sin,cos,tan, exp.. ) also works for matrices.

```
>>a=[1 2; 3 4];
```

```
>> b=sin(a);
```

$$b = \begin{bmatrix} \sin(1) & \sin(2) \\ \sin(3) & \sin(4) \end{bmatrix} = \begin{bmatrix} 0.841 & 0.909 \\ 0.141 & -0.756 \end{bmatrix},$$

```
>> c=exp(a);
```

$$c = \begin{bmatrix} e^1 & e^2 \\ e^3 & e^4 \end{bmatrix} = \begin{bmatrix} 2.718 & 7.389 \\ 20.08 & 54.59 \end{bmatrix}$$

## MATRISLERDE SCALAR CARPMA VE BOLME

**X=a.\*b** , a ve b vectorlerinin scalar carpimini verir.

Normal carpmda kullanilan \* yerine .\* kullanildigina dikkat ediniz.

```
>> a = [ 15 16 12 20 ], b =[ 10 4 6 5 ], x=a.*b
x = [ 150 64 72 100]
```

$$15 * 10 = 150$$

$$16 * 4 = 64$$

$$12 * 6 = 72$$

$$20 * 5 = 100$$

```
>> a = [15 16 12 20 ], b =[ 10 4 6 5 ], y=a./b
```

Normal bolmede kullanilan / yerine ./ kullanildigina dikkat ediniz.

$$y = [ 1.5 4 2 4 ]$$

$$15 / 10 = 1.5$$

$$16 / 4 = 4$$

$$12 / 6 = 2$$

$$20 / 5 = 4$$

```
>>q=[1 2; 3 4], p=[10 20; 30 40]; w=p+q
```

$$p = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}, q = \begin{bmatrix} 10 & 20 \\ 30 & 40 \end{bmatrix}, w = \begin{bmatrix} 11 & 22 \\ 33 & 44 \end{bmatrix}$$

```
>>q=[1 2; 3 4], p=[10 20; 30 40]; z=q.*p, k=p./q
```

$$z = \begin{bmatrix} 10 & 20 \\ 90 & 160 \end{bmatrix}, k = \begin{bmatrix} 10 & 10 \\ 10 & 40 \end{bmatrix}$$

## MATRIS CARPIMLARI

$$\begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \\ b_{31} & b_{32} \end{bmatrix} \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix} = \begin{bmatrix} a_{11}b_{11} + a_{12}b_{21} + a_{13}b_{31} & a_{11}b_{12} + a_{12}b_{22} + a_{13}b_{32} \\ a_{21}b_{11} + a_{22}b_{21} + a_{23}b_{31} & a_{21}b_{12} + a_{22}b_{22} + a_{23}b_{32} \end{bmatrix}$$

$$\begin{bmatrix} 2 & 3 & 4 \\ 5 & 6 & 7 \end{bmatrix} \begin{bmatrix} 10 & 20 \\ 30 & 40 \\ 50 & 60 \end{bmatrix} = \begin{bmatrix} 310 & 400 \\ 580 & 760 \end{bmatrix}$$

```
>>aa=[2 3 4; 5 6 7], bb=[10 20; 30 40; 50 60], x=aa*bb
```

$$x = \begin{bmatrix} 310 & 400 \\ 580 & 760 \end{bmatrix}$$

---


$$\begin{bmatrix} 10 \\ 20 \\ 30 \end{bmatrix} = 200$$

```
>>a=[2 3 4], b=[10 20 30]', x=a*b
x=200
```

---

$$\begin{bmatrix} 10 \\ 20 \\ 30 \end{bmatrix} \begin{bmatrix} 2 & 3 & 4 \end{bmatrix} = \begin{bmatrix} 20 & 30 & 40 \\ 40 & 60 & 80 \\ 60 & 90 & 120 \end{bmatrix}$$

```
>>a=[2 3 4], b=[10 20 30]', x=b*a
```

$$x = \begin{bmatrix} 20 & 30 & 40 \\ 40 & 60 & 80 \\ 60 & 90 & 120 \end{bmatrix}$$


---

$$[2 \ 3 \ 4] [10 \ 20 \ 30] = \text{HATALI ISLEM}$$

```
>>a=[2 3 4], b=[10 20 30], x=a*b
```

**?? Error using ==> mtimes**

**Inner matrix dimensions must agree.**

**Matris boyutlari uyusmazsa carpma tanimsizdir.**

### DIMENSION ERROR

```
>>a=[2 5 4], b=[8 3 12 5]
>>x=a+b
```

**?? Error using ==> plus**

**Matrix dimensions must agree.**

eleman eleman yapılan işlemlerde a ve b aynı boyutta olmalıdır.

x = a\*b, y = a.\*b, z = a/b w=a./b

**hepsi hatalıdır.**

**Ornek 431 : x=0; x=1; x=8 x=5; icin y=3x<sup>2</sup>+5x+7 degerini hesaplayin bir matris halinde gosterin.**

**Method 1.**

```
a1=0; b1=3*a1^2 + 5*a1 + 7
```

```
a2=1; b2=3*a2^2 + 5*a2 + 7
```

```
a3=8; b3=3*a3^2 + 5*a3 + 7
```

```
a4=5; b4=3*a4^2 + 5*a4 + 7
```

```
tt=[a1 b1; a2 b2; a3 b3; a4 b4]
```

```
tt=
```

$$\begin{bmatrix} 0 & 7 \\ 1 & 15 \\ 8 & 239 \\ 5 & 107 \end{bmatrix}$$


---

**Method 2.**

```
aa=[0 1 8 5]
aa_Length=length(aa);
for kk=1:aa_Length,
bb(kk)= 3* aa(kk) ^2 + 5*aa(kk) +7
end;
bb=[7 15 239 107]
```

```
tt=[aa' bb']
```

```
tt=
```

$$\begin{bmatrix} 0 & 7 \\ 1 & 15 \\ 8 & 239 \\ 5 & 107 \end{bmatrix}$$


---

**Method 3.**

```
aa=[0 1 8 5]
bb=3*aa.^2 + 5*aa +7
```

---

**Method 4.**

```
aa=[0 1 8 5]
pol_coef =[3 5 7]
```

```
b1=polyval(pol_coef,0)
```

```
b2=polyval(pol_coef,0)
```

```
b3=polyval(pol_coef,0)
```

```
b4=polyval(pol_coef,0)
bb=[ b1 b2 b3 b4]
```

---

**Method 5.**

```
aa=[0 1 8 5]
pol_coef =[3 5 7]
bb=polyval(pol_coef,aa)
```

---

**Problem:**  $y = 3x^2 + e^{0.1x} - 20 \sin(x)$

Calculate y for x=0, x=0.5 , x=1, and x=2

**Long method:**

```
>>x=0, y = 3*x^2 + exp(0.1*x) -20*sin(x)
1
```

```
>>x=0.5, y = 3*x^2 + exp(0.1*x) -20*sin(x)
-7.78
```

```
>>x=1, y = 3*x^2 + exp(0.1*x) -20*sin(x)
-12.72
```

**Short method**

```
>>x=[0 0.5 1 2],
```

```
>>y = 3*x.^2 + exp(0.1*x) - 20*sin(x)
1 -7.78 -12.72 -4.96
```

Notice **the dot .** in  $x.^2$

**for**

```
>> for kk=1:4, aa(kk)=kk^3; end;
```

```
aa=[ 1^3    2^3    3^3    4^3 ]
```

```
aa=[ 1    8    27   64 ]
```

---

### MATRIS KARESI VE USTEL ISLEMLER

```
>> a=[ 2 5 7 -8 ], b=a^2
```

??? Error using ==> mpower

Matrix must be square.

```
>> a=[ 2 5 7 -8 ], b=a.^2
```

```
b=[ 4 25 49 64]
```

$$2^2 = 4 \quad 5^2 = 25 \quad 7^2 = 49 \quad (-)8^2 = 64$$

```
>> a=[ 2 5 7 -8 ], b=a.^3
```

```
b=[ 8 125 343 -512 ]
```

---

```
>> a=[1 2; 3 4]; d=a.^2;
```

$$d = \begin{bmatrix} 1^2 & 2^2 \\ 3^2 & 4^2 \end{bmatrix} = \begin{bmatrix} 1 & 4 \\ 9 & 16 \end{bmatrix},$$

```
>> g=a.^2
```

$$g = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} 7 & 10 \\ 15 & 22 \end{bmatrix}$$

**a.^2 ile a^2** arasindaki farki gozlemleyin.

---